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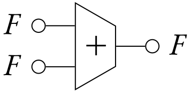
(Closure) 

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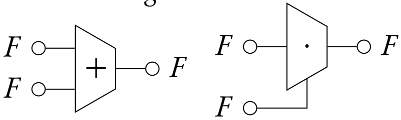
(Closure) 

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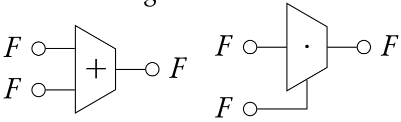

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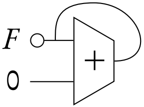

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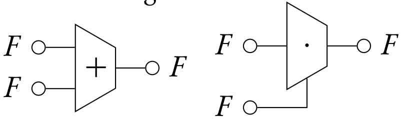

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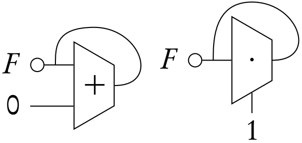

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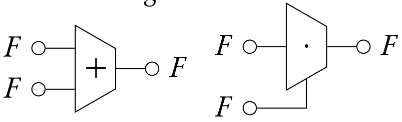

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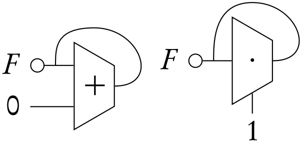

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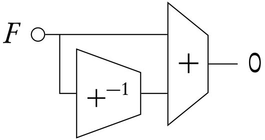

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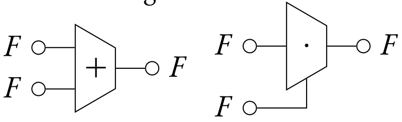

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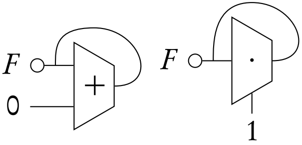

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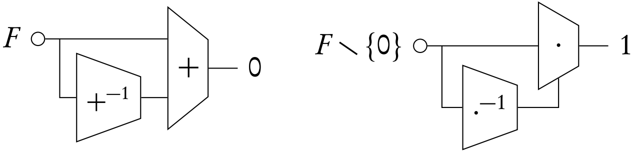

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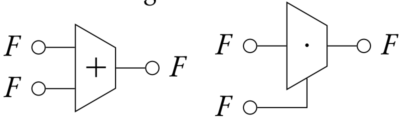

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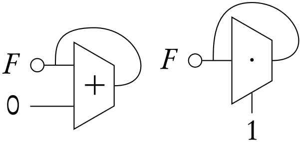

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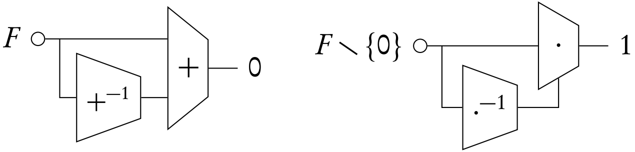

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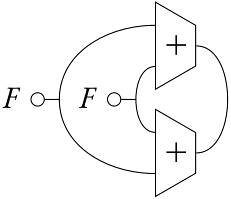

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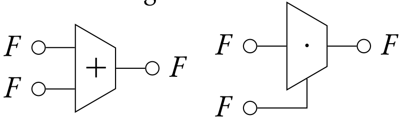

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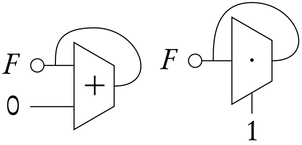

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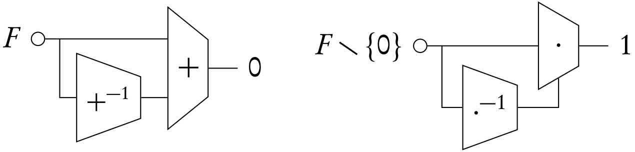

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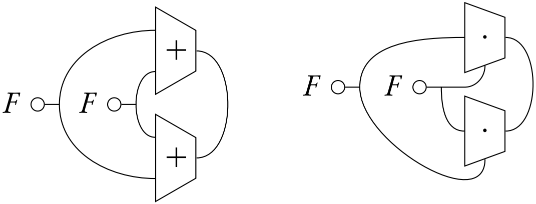

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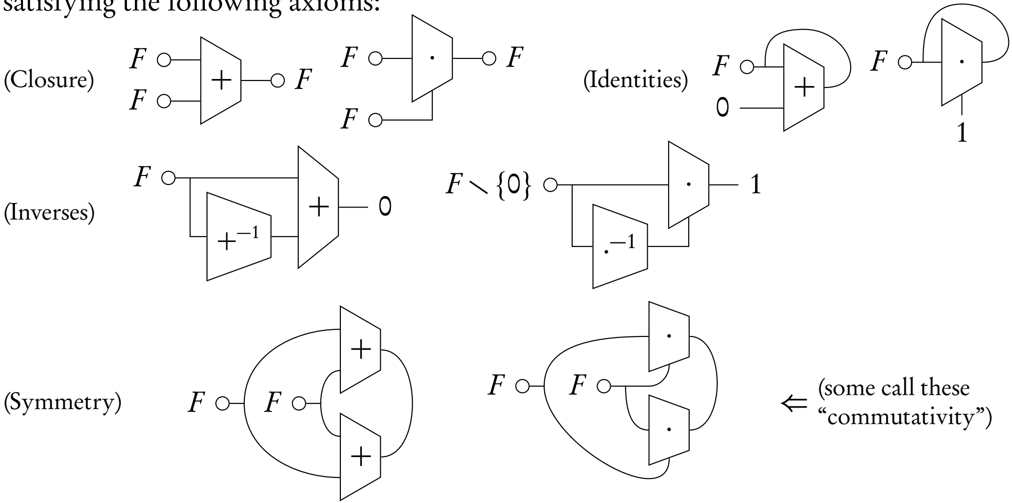

Fields (continued)

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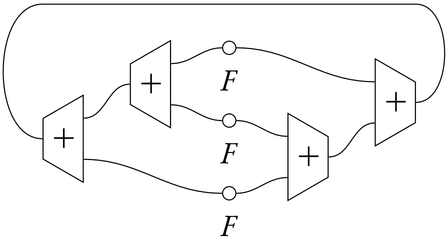

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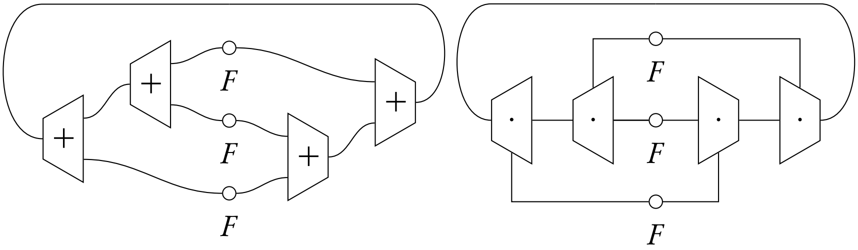

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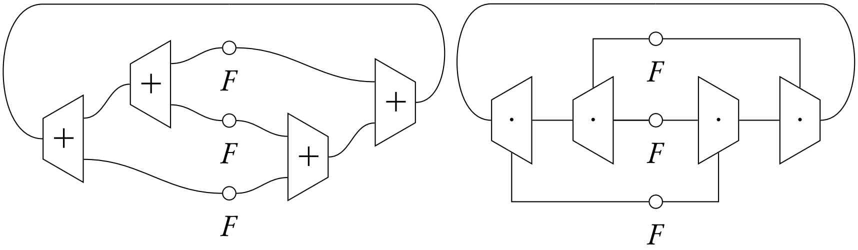

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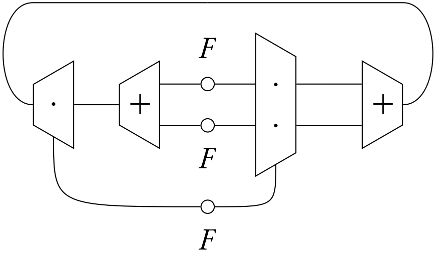

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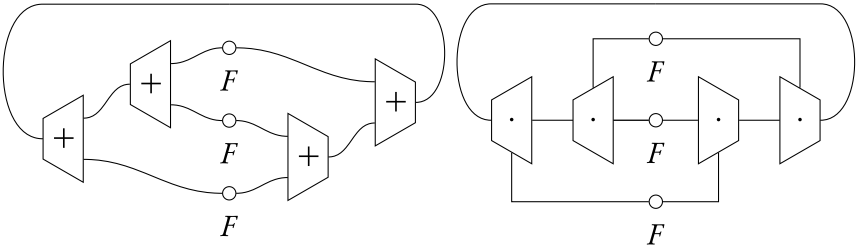

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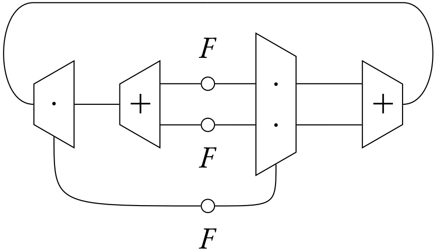

What this really says is that + (addition) and · (scaling) commute with each other!

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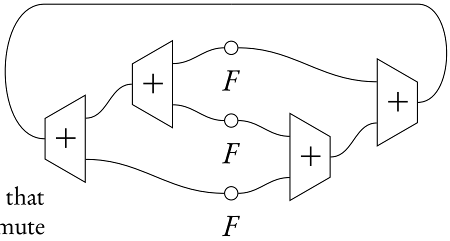

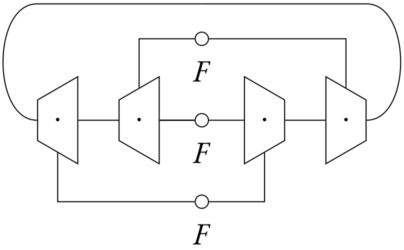

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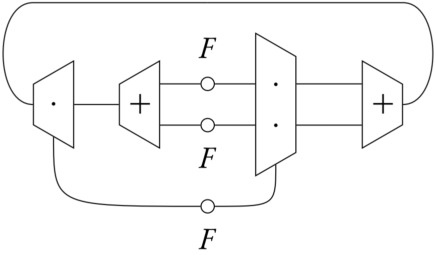

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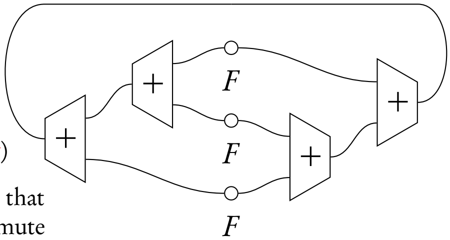

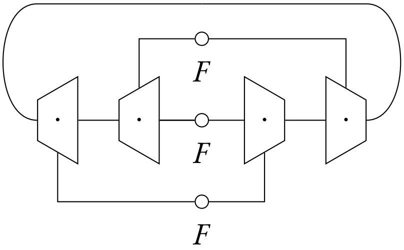

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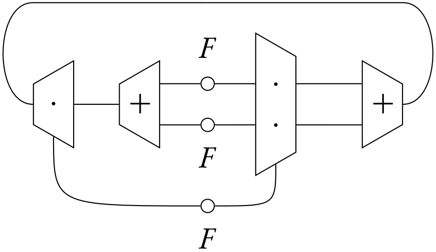

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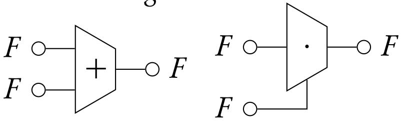

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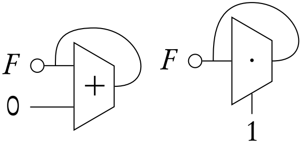

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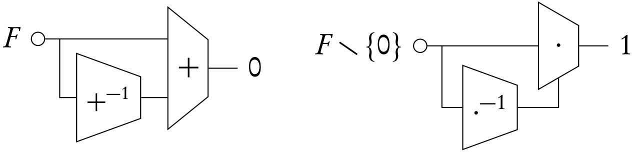

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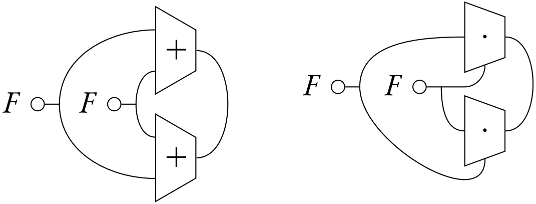

$\Leftarrow$ not really commutativity